

1 The Question

Do systems shaped by **very different optimization** — evolution vs. gradient descent — converge on the same internal organization? Sparse transcoders give the interpretable, neuron-like units to test cortical network signatures inside an LLM.

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cortical signatures
reproduced in an
LLM

16,384

features per layer
Gemma Scope 2, 2
scales

$$d_B \approx 1.35$$

fractal within
modules
(cortex ≈ 2.0)

2 From Features to Networks

Each interpretable **transcoder feature** is a node; edges are co-activation across a corpus — an empirical network read with the network-neuroscience toolbox.

DECOMPOSE

Gemma Scope 2 ·
16,384 features /
layer

CO-ACTIVATE

1M tokens ·
16K×16K Pearson

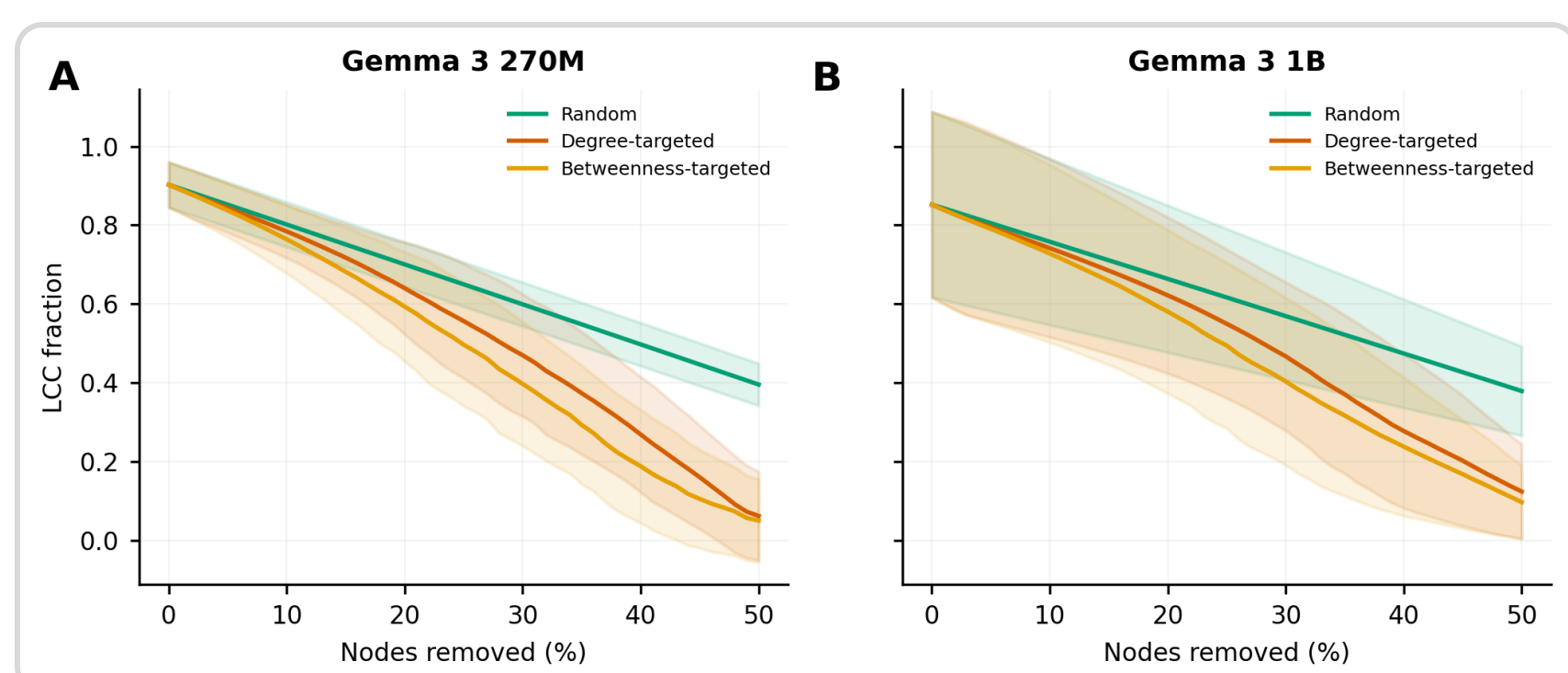
ANALYZE

topology +
Laplacian RG

Gemma 3 **270M** (18L) & **1B** (26L); density-matched $d=0.001$, tested vs. Erdős–Rényi & Configuration-Model nulls. A parallel **structural** network comes from transcoder weights (cosine within-layer, virtual weight across).

3 Structured & Modular

- **Small-world.** $\omega \approx 0$ — clustering with short paths, like cortex.
- **Scale-free hubs.** Degree up to $47\times$ / $53\times$ the mean (270M / 1B).
- **Modularity rises with depth.** Leiden Q : $0.48 \rightarrow 0.88$ / $0.46 \rightarrow 0.93$; null z up to **808**.
- **Built-in control.** Two 1B global-attention layers are clear outliers ($Q=0.09, 0.11$).



Hub vulnerability. Random removal keeps $\approx 40\%$ of nodes at 50% removed; **targeted** hub removal collapses the largest connected component.

4 Same Signatures as the Cortex

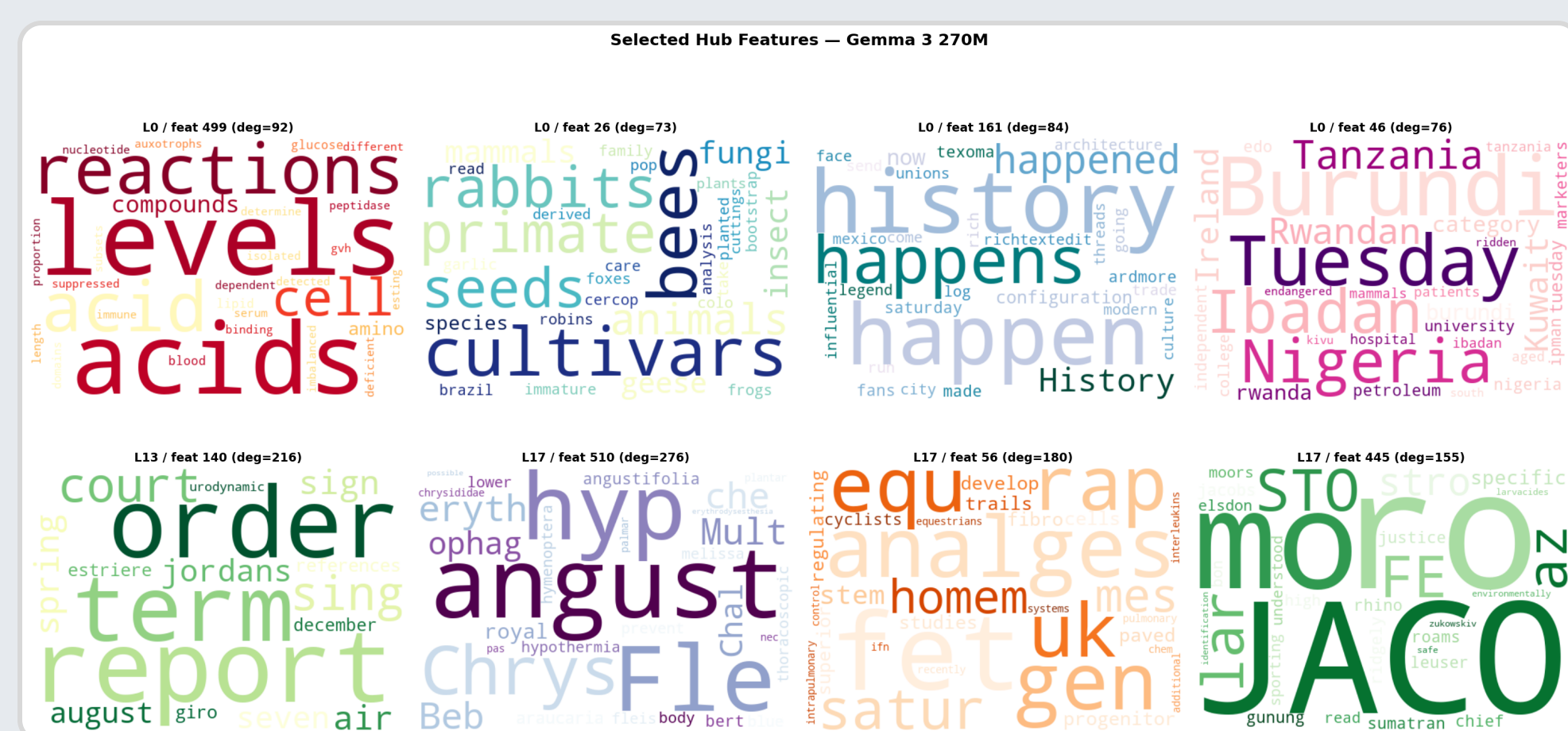
Property	Brain networks	LLM features
Small-world	$\omega \approx 0$	$\omega \approx 0$
Increasing modularity	primary $\rightarrow$ assoc.	early $\rightarrow$ late layers
Fractal in modules	$d_B \approx 2.0$	$d_B \approx 1.35$
Hub vulnerability	hub lesions	hub removal $\rightarrow$ collapse
Structure $\neq$ function	DTI $\neq$ fMRI	cosine $\neq$ Pearson
Scale structure	broad plateau	$C(\tau)$ single peak

Four signatures reproduced across a $4\times$ scale jump; two gaps (lower d_B , **single-peak** vs. plateau spectrum) mark **sparser** wiring.

5 Multi-Scale Structure & Flow

- **Dual-regime fractal.** $d_B \approx 1.35$ within modules (cortex ≈ 2.0), crossover $l_B^* \approx 6$; a single $C(\tau)$ peak sharpens with depth.
- **Structure $\neq$ function.** Mantel $r \approx 0$ globally, yet top-0.1% edges carry **20–25 $\times$** the mean; flow runs focused $\rightarrow$ broadcast $\rightarrow$ focused.
- **Compressible.** Laplacian RG merges up to **38–42 $\times$** (270M) / 62 $\times$ (1B) in deep layers.

6 Topology Carries Meaning



Hubs carry meaning: early-layer content words (top) → mega-hubs (34–47x) → digits → late-layer morphological roots (bottom).

Different optimizers, similar networks: transformer feature networks share several statistical signatures with cortex — a basis for *network-theoretic* interpretability.